Ki-Pode: Keypoint-based Implicit Pose Distribution Estimation of Rigid Objects



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1. Motivation

Pose estimation is the task of recovering an object's 3D rotation and 3D translation. Prior work has primarily been concerned with the estimation of a single best estimate. However, object poses are often ambiguous e.g. due to symmetry or occlusion. Since pose ambiguity cannot be expressed by a single pose estimate, we estimate an entire probability distribution over object poses. As our primary concern was reliability, our method provides distribution estimates which are expressive, conservative, and interpretable.

Expressive: We express the pose distribution using an implicit formulation since this allows our method to model distributions of arbitrary complexity. **Conservative**: Estimates must be conservative since overconfident estimates can lead to false positives, resulting in an unreliable system. **Interpretable**: Since our method is trained on synthetic data, it is valuable to have interpretable estimates, to aid in identifying if the sim-to-real domain transfer is successful.



Pose from keypoints

The probability distribution over the pose θ can be expressed in terms of a joint distribution over projected keypoints \mathbf{k}_{θ} . Since the projected keypoints uniquely define a pose, it can be derived that:

$$p(\theta|I) = \int p(\theta|\mathbf{k}, I) p(\mathbf{k}|I) d\mathbf{k}$$
$$= p(\mathbf{k}_{\theta}|I)$$



Joint to marginals

The joint keypoint distribution is approximated from the marginal distributions, using the assumption of **strong correlation** $(p(k_i, k_j) =$ $p(k_i))$. This approximation is conservative since error introduced by the approximation will overestimate regions of low probability:

Heatmap estimation

The marginal distributions, referred to as a heatmap, are estimated using a **U-Net**[1]. The problem is formulated as **spatial classification** and the network is trained using cross-entropy loss with the target distributions being isotropic Gaussians.

Normalization

SO(3) is sampled in an equivolumetric grid using the Healpixbased method in [2]. The unnormalized likelihood is estimated for the M samples, interpreted as probability, and normalized such that the normalized likelihood can be computed as:

$\hat{\mathbf{p}}(\theta_{i}|I) \approx \hat{\mathbf{P}}(\theta_{i}|I) / (\pi^{2}/M)$





$$L = -\sum_{i=1}^{N} \mathcal{N}(k_i, \sigma) \log \hat{p}(k_i | I)$$

$$\prod_{i=1}^{N} \prod_{i=1}^{N} \prod_{i$$

3. Results

Our method has been applied to orientation estimation, so it can be compared to existing works. The figure shows our method applied to three objects. With 5 HEALPix recursions (1.8 million samples) the computation time was \sim 125ms. The mean log-likelihood of the ground truth pose is used as a metric for comparison. Our method achieves state-of-the-art results on the YCB-V dataset and modest results on the T-LESS dataset. Furthermore, our method performs reliably on all objects.



4. Conclusion

We have presented a novel pose distribution estimation method, which provides estimates that:

- rely on conservative approximations to ensure reliability
- are highly expressive due to being formulated implicitly
- have high interpretability due to the intermediary keypoint representation

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$\mathbf{YCB-V}$

| | Summary of Evaluation in [3] | | | | |
|-------------------|------------------------------|-------|-------|-------|----------------|
| | I | II | III | IV | Ki-Pode (ours) |
| master chef can | -0.78 | -1.66 | 2.32 | 0.09 | 4.36 |
| cracker box | 4.03 | 3.75 | -0.09 | 3.71 | 6.05 |
| sugar box | 3.77 | 5.94 | 2.62 | 4.20 | 6.47 |
| tomato soup can | 0.90 | 2.02 | 2.52 | 3.99 | 5.16 |
| mustard bottle | 3.85 | 4.61 | 3.02 | 4.81 | 5.45 |
| tuna fish can | -3.12 | -0.20 | 2.64 | 1.23 | 5.10 |
| pudding box | 2.18 | 2.64 | 3.13 | 4.54 | 4.91 |
| gelatin box | 4.65 | 6.25 | 3.53 | 5.73 | 6.35 |
| potted meat can | 1.18 | 3.28 | 1.60 | 3.06 | 3.11 |
| banana | 2.58 | 0.58 | 2.27 | 3.70 | 4.80 |
| pitcher base | 3.34 | 4.68 | 2.35 | 4.88 | 5.39 |
| bleach cleanser | 3.91 | 4.70 | 2.29 | 3.38 | 4.02 |
| bowl | 1.37 | -2.77 | -1.21 | -9.62 | -1.50 |
| mug | 3.73 | 2.50 | 2.75 | 4.72 | 4.62 |
| power drill | 4.31 | 5.92 | 2.43 | 4.17 | 6.14 |
| wood block | 2.64 | -2.09 | -0.51 | 4.49 | -1.76 |
| scissors | 3.74 | 0.51 | 0.66 | 1.63 | 5.49 |
| large marker | -7.59 | -0.29 | 1.02 | -8.13 | 3.94 |
| large clamp | -5.64 | -6.67 | -1.63 | -3.54 | 3.07 |
| extra large clamp | -5.20 | -2.92 | 0.19 | -5.03 | 2.25 |
| foam brick | -0.26 | -2.28 | 1.70 | -12.0 | 2.44 |
| All | 0.86 | 1.71 | 1.74 | 1.43 | 4.09 |

T-LESS

| Deng^1 | 5.3 |
|-----------------------|-----|
| $ m Gilitschenski^1$ | 6.9 |
| Prokudin ¹ | 8.8 |
| $IPDF^1$ | 9.8 |
| Ki-Pode (ours) | 3.3 |

¹Results published by Murphy et al. [4]



6. References

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