# PAUMER: Patch Pausing Transformer for Semantic Segmentation

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#### Abstract

We study the problem of improving the efficiency of segmentation transformers by using disparate amounts of computation for different parts of the image. Our method, PAUMER, accomplishes this by pausing computation for patches that are deemed to not need any more computation before the final decoder. We use the entropy of predictions computed from intermediate activations as the pausing criterion, and find this aligns well with semantics of the image. Our method has a unique advantage that a single network trained with the proposed strategy can be effortlessly adapted at inference to various runtime requirements by modulating its pausing parameters. On two standard segmentation datasets, Cityscapes and ADE20K, we show that our method operates with about a 50% higher throughput with an mIoU drop of about 0.65% and 4.6% respectively.

#### **1** Introduction

Vision transformers [**b**, **C**] (ViT) have recently demonstrated very strong performance on large scale image classification tasks. These networks break the images into a collection of patches (or tokens, interchangeably) and progressively refine their representation by processing them through a series of residual self-attention layers [**C**]. While their genesis was for image classification, recent methods have adapted transformer architectures to various computer vision tasks [**D**, **C**], **C**], and specifically to semantic segmentation [**C**], **C**], **C**].

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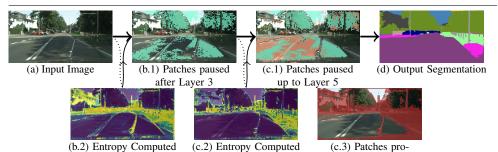


Figure 1: Illustration of our proposed method. Our method prossed strikely stops processing patches after they reach a low enough prediction entropy. First column (a) shows the input image. Second column (b.1) shows the patches that are stopped from being processed after the third transformer layer in green. Third column shows additional patches that are paused after the fifth layer in pink. In the bottom row, (b.2) and (c.2), we show the entropy computed from the auxiliary decoders that is used to decide which patches to pause (Section 2.1). It is apparent that the network automatically pauses easy parts of the image while allocating more computation to the parts that correspond to boundaries, and to smaller and rarer classes, as shown in (c.3) in red. Figure best viewed on a reader with zooming capability. Full details are presented in Section 2.

In this work, we are interested in patch dropping in the context of semantic segmentation. Differing from the case of image classification, it is not possible to drop patches in semantic segmentation, as we have to predict the labels for all the pixels. Instead, we redefine the problem in the context of semantic segmentation to *patch pausing*: pausing a patch at a certain layer signifies that its representation is not going to be updated by any subsequent encoder layer, it does not contribute to the feature computation of other patches, and it is fed directly to the decoder. Consider segmenting natural road scenes from Cityscapes [I] in Figure 1, it is apparent that some parts of the scene are relatively simpler to segment (say, the sky, and the road). So, we allocate lesser computation power to these patches by pausing their feature computation, and feed them as-is to the decoder to produce the final segmentation map. Our argument is supported by the findings in Raghu et al. [II]; they find that the representations of tokens is primarily modified in the first half of the network, and relies on the residual connections to only marginally refine them in the later stages. This opens up an opportunity to reuse the representations, instead of recomputing them, and thus improving the efficiency of segmentation transformers.

Our criterion for token pausing is the time-tested posterior entropy of the segmentation labels. We find that entropy is strongly indicative of lower error. Our method, called Patch pAUsing segmentation transforMER (PAUMER), adds a simple linear auxiliary decoder to predict labels and compute entropy, and processes only the patches whose class prediction is of high entropy, *i.e.* the network is not confident about predicting the labels of these patches, and processes them more. Based on the Segmenter [2] architecture, we show the performance of our method on the standard benchmark suite of ADE20K [5] and Cityscapes [5]. Our method pushes the pareto front of the speed-accuracy trade-offs, and we find that we can operate at a 50% higher throughput with a drop in mean intersection of union of 4.6% and 0.65% on ADE20K and Cityscapes respectively, and for doubling the throughput, the drop is about 10.7% and 4.5% respectively.

## 2 Patch pausing transformer for Semantic Segmentation

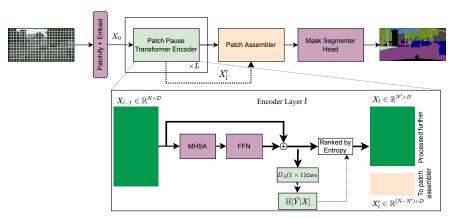


Figure 2: Schematic of our proposed method. We modify Segmenter [22] to enable pausing of patches, and feeding them directly to the decoder. Our proposed PAUMER encoder adds a simple auxiliary decoder (a  $1 \times 1$  convolution), and uses the predicted posterior entropy  $\mathbb{H}[\hat{Y}|X]$  of each component of X to reorder the feature representation X. A portion ( $\tau$ ) of this feature representation would be paused and fed to the decoder directly. The rest of the features (of size N' < N) are processed further.

Patch pausing for semantic segmentation is tied to the notion that computation should be non-uniformly distributed across the image, with some parts of the input needing more computation than others to obtain an accurate segmentation. This notion is difficult to realize in the case of convolutional networks as convolution implementations in popular deep learning frameworks handle only inputs with uniform coordinate grid, and thus need software optimizations [ $\square$ ], or require architectural simplifications like the use of  $1 \times 1$  convolutions in the network [ $\square$ ]. On the other hand, ViTs are ideally suited for this purpose, as each transformer layer consumes a matrix of patch representations without any regard to its inputs spatial location. Removal of patches from computation does not require any additional modifications to the transformer networks for them to apply heterogeneously distributed computation across an image. This restricts the pausing pattern to operate at a patch level, and these paused patches can be non-uniformly distributed over the image coordinate grid. Our primary experiments are based on the architecture Segmenter [ $\square$ ], which uses a ViT backbone to extract patch representations, and predicts a segmentation map using a transformer-based mask decoder. We describe this in detail in Appendix C

#### 2.1 Using Entropy as a criterion for patch-pausing

How do we determine which tokens to pause, *i.e.* which one do not need more processing? Consider the unrealistic case when we have access to the ground truth labels. We could decode after each layer  $l \in \{1 \dots L\}$ , and stop the processing of tokens for which the prediction is accurate enough.

In the absence of ground truth to determine which tokens can be paused, we propose to use the entropy of label predictions as a proxy for the correctness of the network's predictions. We posit that our models, when confident about their prediction, are likely to be correct. To sanity-check the aptness of entropy as a pausing criterion, we plot in Figure 3 the

entropy of predictions computed after every second layer in a segmenter. Specifically, we use a Segmenter with ViT-Ti backbone pretrained on Cityscapes, freeze its weights, and only train the one-layer linear auxiliary predictor added after each layer. Each vertical plot is a histogram, and we see that in the initial layers, there is a higher overlap of correct and incorrect predictions' entropies. When a token has been processed enough to predict the correct label, the entropy of the prediction is generally low. Thus, pausing patches based on entropy results in representations that have been refined enough to result in correct predictions.

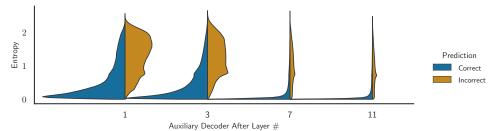


Figure 3: Violin plot of entropy of predictions at intermediate layers. In this figure, we plot the entropy distribution of the auxiliary predictions for 10% of images in Cityscapes validation set. The x-axis marks after which layer the prediction was done. For each layer, the entropy distribution is shown for tokens correctly (in blue) and incorrectly (in orange) classified. We see that the entropies of the predictions for tokens correctly classified accumulate in the low values in the later layers (blue spike on the bottom-right)

#### 2.2 Training PAUMER- One training for many pause configurations

We base our network on Segmenter's architecture [ $\square$ ] detailed in Appendix C. A pause configuration (or configuration) refers to the proportion of patches paused at each layer of the network. An obvious method is to train and test the same patch pausing configuration that satisfies our run-time requirements. Any changes to the run-time requirements requires retraining the network. For this reason, we propose a more general strategy that enables multiple patch pausing configurations at inference with just one trained model. For each transformer layer *l*, we define a range of patch pausing proportions ( $\tau_l^{\text{lo}}, \tau_l^{\text{hi}}$ ). For each batch of training samples, we sample uniformly one layer  $l \in \{3, ..., L\}$  and a patch pausing proportion  $\tau_l \sim \mathcal{U}[\tau_l^{\text{lo}}, \tau_l^{\text{hi}}]$ , where  $\mathcal{U}$  refers to a uniform distribution over the parameters. To facilitate the patch pausing, we employ a single auxiliary decoder  $D_A$ , parametrized by a  $1 \times 1$  convolution, after the operations of layer *l* (see Figure 2).

The outputs of the main branch of the network and the auxiliary branch are trained using the traditional cross entropy loss.

$$\mathcal{L}_{\text{main}} = \text{CE}(\mathbf{y}, \hat{\mathbf{y}}) \tag{1}$$

$$\mathcal{L}_{aux}^{l} = CE(\mathbf{y}, \hat{\mathbf{y}}^{l}) \tag{2}$$

where y is the ground truth,  $\hat{y}$  refers to the logits predicted by the main decoder (mask transformer), and  $\hat{y}^l$  is the auxiliary decoder's output at the l<sup>th</sup> layer. The total loss used to train is a combination of losses in Equations (1) and (2).

$$\mathcal{L}_{\text{total}} = \mathcal{L}_{\text{main}} + \lambda \mathcal{L}_{\text{aux}}^{i} \tag{3}$$

where  $\lambda$  is a scalar used to scale the contribution of additional losses.

At layer *l*, entropy is computed for each component of  $X_l$  as

$$H_l \coloneqq \mathbb{H}[\hat{Y}_l|X_l] = \mathbb{H}[\sigma(D_A(X_l))], \tag{4}$$

where  $\sigma$  is the softmax function applied to each pixel independently. With this entropy, we pause the computation of a proportion  $\tau_l$  of tokens with the lowest entropy and store them as  $X'_l$ , and continue with the computation using the rest of the tokens  $X_l$  (see Figure 1). Note that there are other ways to use  $H_l$  to pause tokens, for example by using a threshold on entropy. However, doing so results in pausing and removing different amounts of tokens in each image of a batch, which would add a substantial overhead as padding is not processed efficiently on a GPU. Additionally, pausing a fixed amount of tokens allows for a deterministic computation time.

In order to re-assemble in the original order the patches that have been fully processed and the ones that have been paused, we use a patch assembler module (see Appendix A for PyTorch-like code). It takes  $X_L$  and  $X'_l$ , and reassembles them into the original shape of  $X_0$ . In order to do so, pausing mechanism stores the indices of the patches that have been chosen to be paused, in addition to the current feature representation. The assembler copies the paused representation into the same indices stored previously. This re-assembled output is finally fed into the decoder (mask segmenter head) to compute the segmentation map.

**Inference** Our training procedure of randomized pause configurations gives us the advantage to choose a pausing configuration that is informed by the run-time requirements *i.e.* mIoU and number of images processed per second. This configuration can have multiple pause locations, each with different pause proportions. We show some results for some configurations listed in Table 1. The patch assembler accordingly assembles multiple paused patches  $\{X'_l\}$ , and the final representation  $X_L$ . The specific configurations are chosen to display the adaptability of the trained network to various inference time requirements, and do not hold any specific importance. Pause configurations can be added easily, as it does not influence the training, but only requires testing over the validation set.

## **3 Related Work**

We now discuss some important prior work related to our method, before showing the experimental evidence.

Segmentation using Transformers Transformers that were originally proposed for language processing tasks [26] have been incorporated into vision [ $\Box$ ,  $\Box$ ] and several improvements have been proposed [ $\Box$ ]. SETR [ $\Box$ ] adapted the standard vision transformer (ViT) to segmentation by using multiscale decoder on all the image patches. Segmenter [ $\Box$ ] improved the decoder design by using a learnable per-class token that acts as weighting mechanism over the tokens' representations. Segformer [ $\Box$ ] redesigned the architecture with a multiscale backbone that does not use positional encoding, and an MLP based decoder. Several improvements to the transformer backbone have been shown to have impact on the down-stream segmentation performance [ $\Box$ ,  $\Box$ ,  $\Box$ ,  $\Box$ ,  $\Box$ ]. These improvements to the transformer backbone have been shown to have impact on the second, number of floating point operations per second (FLOPs), or images processed per second.

**Token sparsification methods** Several components of the whole transformer architecture have been improved, by approximations, and simplifications to attention mechanism. Interested readers can refer to Tay et al. [23]. Orthogonal to the architectural improvements,

recent work has focused on the reduction of the data processed, and our proposed method is a form of input dependent reduction. Graves [1] proposed Adaptive Computation Time (ACT), where the amount of processing for each input to an RNN is decided by the network by determining a halting distribution. It was adapted to residual networks by Figurnov et al. [2], that dynamically decides to apply differential number of residual units to different parts of the input. This has been adapted to transformers too  $[\Box 2]$ , where the tokens are progressively halted as they are determined have been processed enough according to a similar criterion as ACT. DynConv [22] uses an auxiliary network to predict pixel masks using which indicate pixels of the image that are not processed by a residual block. DynamicViT [22] extends this formulation to transformers where they, similarly, use an auxiliary network to predict which patches are dropped from being refined further. The auxiliary branches are trained using the Gumbel-softmax trick [III] in both these methods. We consider simplicity of the steps the strength of our proposed method. Unlike DynamicViT [22], we do not need techniques like Gumbel-softmax that are harder to optimize, and additional tailored losses. Additionally, both A-ViT and DynamicViT drop a fixed amount of patches for a given image, and do not provide the flexibility to vary the number of patches dropped, as our method does.

Early-exit methods Dynamic neural networks [9] adapt the architectures or parameters in an input adaptive fashion. Specifically, early-exit methods find that deep neural networks can overthink where a network can correctly predict before all layers process the input, and it can even result in wrong predictions due to over-processing [1]. Several methods to determine when to exit the network have been proposed. Branchynet [22] and Shallow-Deep nets [III] uses auxiliary classifiers to predict the output class for vision convolutional networks, and stops processing a sample if the entropy of a branch's predictions is lower than a predefined threshold. This idea was further exploited in NLP literature. Zhou et al. extends this by using a patience parameter that tracks number of auxiliary classifiers which predict the same class. DeeBERT [11] proposes a two stage training, where the auxiliary decoders are trained after the main networks is trained, and frozen. Li et al. [1] propose a layer cascade for convolutional segmentation networks, that processes easy to hard parts progressively through the network. Their method needs modifications of the network architecture, whereas we show that our proposed method can be added with very little efforts. Our method is an early exit strategy, specifically for the case of segmentation transformers. While similar methods have been examined in literature, to the best of our knowledge, we are the first to examine the patch pausing problem of semantic segmentation. Also, the randomized training presented in Section 2.2 has not been used in this context, though similar ideas to reduce network width were studied in slimmable networks [33].

#### 4 **Experiments**

#### 4.1 Datasets and Evaluation

We show the performance of our method using networks trained on Cityscapes [I] and ADE20K [I]. Cityscapes (CS) consists of 2,975 images in the training set, in which each pixel belongs to one of 19 classes, and 500 images in the validation set which are used to benchmark the performance of our method. ADE20K is substantially larger, with a training set of 25,574 with 150 classes, and 2,000 images to validate the performance. The results for Cityscapes and ADE20K are presented below.

Our primary performance measure is based on the speed-accuracy trade-off, measured

by mean Intersection over Union (mIoU) metric and throughput in images per second. To determine the number of images processed per second (IMPS), following Strudel et al. [ $\Box a$ ], we use images of size  $512 \times 512$  with a batch size that optimally occupies a V100 GPU.

**Methods compared** To assess the performance of our proposed method, we use the following baselines for comparison:

- a. Baseline set by Segmenter, without any patch pausing.
- b. **Random Pausing (RP)**: We train the network to handle pausing a proportion  $\tau$  of randomly chosen patches, instead of the lowest entropy ones.

We examined an additional simple baseline of random pausing (without training), and found the results not competitive enough to warrant reporting here. Also, some methods in Section 3 are capable of dropping different patches per image. These methods can result in a decrease in FLOPs (floating point operations), but this reduction cannot be realized in wall clock improvements as modern GPUs parallelize computation over batch elements.

ayer	Pause configurations													
Pause La	3 5 7	0.2	0.4	0.6	0.2	0.4	0.6	0.8	0.2 0.2	0.3 0.3	0.4 0.4	0.2 0.2 0.2	0.3 0.3 0.3	0.4 0.4 0.4

Table 1: Table of configurations. Each column represents a pause configuration, *e.g.* the first column represents the configuration pausing 20% of tokens after layer 3, using the notation introduced in Section 2.2. Each configuration here corresponds to a marker in Figures 4a, 4b and 13.

**Training hyperparameters and Inference Configurations:** For our main experiments, we use Segmenter with ViT-Ti and ViT-S backbones (details in Appendix B). During training, we follow the procedure in Section 2.2 for every network and dataset, and in particular we pause a random amount of tokens  $\tau_l \sim \mathcal{U}[0.2, 0.8]$  at a random layer  $l \in \{3, 4, 5, 6, 7, 8, 9\}$ . We initialize the model for our training with pretrained segmenter weights, as we find this results in better performance, and train the model for 80,000 steps for Cityscapes and 160,000 steps for ADE20K. The auxiliary loss-weight  $\lambda$  is set to 0.1. Rest of the hyperparameters as kept the same as in Strudel et al. [22]. We implement our method using mmsegmentation [3], and use their pretrained models whenever available. At inference, we test the networks with the pause configurations in Table 1. This list of pause configuration is not exhaustive, and does not hold any specific importance, but have been chosen to show the efficiency of our method in trading off mIoU for higher IMPS.

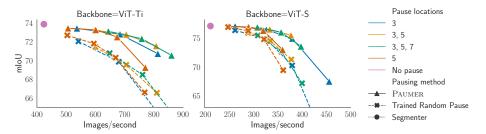
**Choosing pause configurations:** Determining the appropriateness of a pausing configuration incurs little additional cost, as it only requires inference with a validation set for each configuration of interest (see Figures 4a and 4b). On a new dataset for which we train the network with the proposed training procedure, we foresee two scenarios:

- 1. If the objective is to attain a specific throughput, we can easily find configurations that match the requirement with a sweep over them (Figures 9 and 10) by only timing them, and then evaluating the mIoU of the ones that meet the time requirement.
- 2. If the objective is to find a good throughput-mIoU trade-off: First, we sweep through configurations that pause at only one layer (Figure 9) and we pick the first layer and

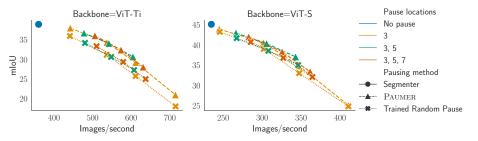
proportion. We fix this layer and ratio, then sweep through pausing configurations at a second layer (Figure 10). We repeat this procedure until adding more layers is no longer beneficial.

#### 4.2 Results

**Performance analysis** In Figure 4a, we plot the mIoU versus the number of images per second achieved by baselines and our entropy patch pausing for different configurations, for Cityscapes. Each point is the average value of three training runs. The left-most point corresponds to the original Segmenter model, in solid line our proposed pausing strategy, and in dashed line random pausing with training. For both ViT-Ti and ViT-S backbones, a 50% increase of IMPS can be achieved with an mIoU drop of about 0.7% and 0.6% respectively. Further, for doubling the IMPS, we see that the mIoU drops about 3.2% and 5.9% respectively. For the trained random pausing using ViT-Ti, a strong baseline, the equivalent drops in mIoU are about 2.9% and 8.8% to increase the IMPS by 50% and 100%, respectively. We show results for ViT-Ti and ViT-S for ADE20K in Figure 4b. For ViT-Ti backbone, we



(a) mIoU vs Images processed per second for ViT-Ti and ViT-S backbones on Cityscapes val set.



(b) mIoU vs Images per second for ViT-Ti and ViT-S backbones on ADE20K val set.

Figure 4: Results on Cityscapes and ADE20K for our proposed method PAUMER. Each marker is a configuration from Table 1. We train a single model capable of handling various pause configurations that can be chosen based on run-time requirements. It is apparent that ADE20K suffers from a higher drop in performance when patch pausing is employed. However, PAUMER consistently outperforms the random training baseline.

see that for a 50% increase in IMPS, mIoU drops by about 2.8%, and a 100% increase in IMPS with a mIoU drop of about 10.7%, compared to random pausing performance of 5.4% and 13.5%. The drop in mIoU is in contrast with the results of Cityscapes, where we could achieve similar increase in throughput with a much lesser drop in performance. We chalk this difference up to dataset characteristics; ADE20K has almost an order of magnitude more

classes, and the images are smaller with cluttered scenes and numerous small objects, which may require more processing to be correctly classified.

Generating these performance plots *i.e.* mIoU vs IMPS is inexpensive, as no retraining is involved and only needs inference on a validation set with reasonably chosen pause configurations.

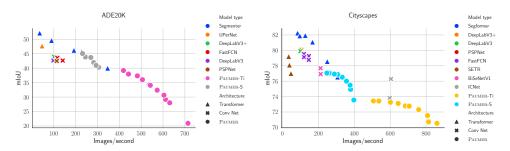


Figure 5: Performance comparison for ADE20K and Cityscapes. We compare to pretrained models available in mmsegmentation [] for each of these datasets. Architectures devised for speed or accuracy outperform us on those criteria, but PAUMER has the unique advantage that we can trade off one for the other using a tunable hyperparameter. Here, we show the pareto front of PAUMERWe use different colors for different architectures, and different shapes for architectural families.

**Comparison to other architectures** In Figure 5, we compare our method to a broad array of architectures for which pretrained models are available in mmsegmentation [**J**]. Here we plot only the best performances obtained for each throughput across pause configurations. We estimate this by computing the skyline queries. We include both convolution based architectures, and transformer based ones. In the transformer family, available networks have focussed on improving the performance, and thus are slower, but more accurate than the PAUMER family of models. CNN based ones (say ICNet for Cityscapes) that have been designed to be more efficient are competitive or better in speed than our models. However, we have the unique ability to tune the mIoU-throughput scores of our model without having to retrain them.

## 5 Discussion

The improvement in images processed per second is obtained by reducing the number of patches processed. This might not necessarily hold true in the case of networks with convolutional layers interspersed, such as SegFormer [23] that uses convolution instead of positional encoding, as convolution on unstructured sparse inputs is not highly optimized in CUDA implementations. Thus, our method is not readily applicable to all transformer models.

In addition to architecture dependence, patch pausing's performance maybe dependent on the dataset itself. We attributed the difference between Cityscapes and ADE20K to inherent dataset complexities by examining the performance of the auxiliary classifier; for ViT-Ti, it reaches around 60% accuracy for ADE20K and 90% accuracy for Cityscapes. Examining the possible relationship between patch pausing performance and the dataset difficulty [**f**] might shed some light on this issue. Additionally, patch pausing assumes that a paused token is not important to the feature computation of other tokens, as it will not contribute further to the attention computation to refine the representation of other patches. Performance (mIoU) indicates that it might have little bearing, but this assumption needs to be investigated further.

Our method, while being input adaptive in choosing the patches to pause, chooses a fixed proportion of them. This design is to exploit the batch level parallelism on GPUs. Choosing the number of patches depending on the input batch has not been dealt with in this paper.

## 6 Conclusion

Our method, PAUMER, is a first step in the direction of post-hoc design for efficient inference in semantic segmentation transformers. We do so by applying dissimilar amounts of computation to various patches of an input image. Patches with high predicted auxiliary entropy are processed further, whereas the rest of them are fed directly to the decoder skipping all the intermediate computation. To run at a specified throughput (images per second), our method offers the flexibility to choose an appropriate pause configuration, without having to retrain the network.

Acknowledgements Evann Courdier and Prabhu Teja are supported by the "Swiss Center for Drones and Robotics - SCDR" of the Swiss Department of Defence, Civil Protection and Sport via armasuisse S+T under project No 050-38.

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